### (A) Main Concepts and Results

- Rectangle
  - (a) Area = length  $\times$  breadth
  - (b) Perimeter = 2 (length + breadth)
  - (c) Diagonal =  $\sqrt{\left(\text{length}\right)^2 + \left(\text{breadth}\right)^2}$
- Square
  - (a) Area =  $(side)^2$
  - (b) Perimeter =  $4 \times \text{side}$
  - (c) Diagonal =  $\sqrt{2}$  × side
- Triangle with base (b) and altitude (h)

Area = 
$$\frac{1}{2} \times b \times h$$

- Triangle with sides as a, b, c
  - (i) Semi-perimeter =  $\frac{a+b+c}{2}$  = s
  - (ii) Area =  $\sqrt{s(s-a)(s-b)(s-c)}$  (Heron's Formula)
- Isosceles triangle, with base a and equal sides b

Area of isosceles triangle = 
$$\frac{a}{4}\sqrt{4b^2 - a^2}$$

Equilateral triangle with side a

Area = 
$$\frac{\sqrt{3}}{4}a^2$$

Parallelogram with base b and altitude h

Area = bh

Rhombus with diagonals  $d_1$  and  $d_2$ 

(a) Area = 
$$\frac{1}{2}d_1 \times d_2$$

(b) Perimeter = 
$$2\sqrt{d_1^2 + d_2^2}$$

Trapezium with parallel sides a and b, and the distance between two parallel sides as h.

Area = 
$$\frac{1}{2} (a + b) \times h$$

Regular hexagon with side a

Area =  $6 \times$  Area of an equilateral triangle with side a

$$= 6 \times \frac{\sqrt{3}}{4} a^2 = \frac{3}{2} \sqrt{3} a^2$$

## (B) Multiple Choice Questions

Write the correct answer:

Sample Question 1: The base of a right triangle is 8 cm and hypotenuse is 10 cm. Its area will be

- (A) 24 cm<sup>2</sup>
- (B) 40 cm<sup>2</sup>
- (C) 48 cm<sup>2</sup>
- (D) 80 cm<sup>2</sup>

**Solution**: Answer (A)

#### **EXERCISE 12.1**

- 1. An isosceles right triangle has area 8 cm<sup>2</sup>. The length of its hypotenuse is
  - (A)  $\sqrt{32}$  cm
- (B)  $\sqrt{16}$  cm (C)  $\sqrt{48}$  cm
- (D)  $\sqrt{24}$  cm

- 2. The perimeter of an equilateral triangle is 60 m. The area is
  - $10\sqrt{3} \text{ m}^2$

- (B)  $15\sqrt{3} \text{ m}^2$  (C)  $20\sqrt{3} \text{ m}^2$  (D)  $100\sqrt{3} \text{ m}^2$
- 3. The sides of a triangle are 56 cm, 60 cm and 52 cm long. Then the area of the triangle is
  - 1322 cm<sup>2</sup> (A)
- (B)  $1311 \text{ cm}^2$
- (C) 1344 cm<sup>2</sup>
- (D) 1392 cm<sup>2</sup>
- **4.** The area of an equilateral triangle with side  $2\sqrt{3}$  cm is
  - (A) 5.196 cm<sup>2</sup>
- (B)  $0.866 \text{ cm}^2$
- (C) 3.496 cm<sup>2</sup>
- (D) 1.732 cm<sup>2</sup>
- 5. The length of each side of an equilateral triangle having an area of  $9\sqrt{3}$  cm<sup>2</sup> is
  - (A) 8 cm
- (B) 36 cm
- (C) 4 cm
- (D) 6 cm
- **6.** If the area of an equilateral triangle is  $16\sqrt{3}$  cm<sup>2</sup>, then the perimeter of the triangle
  - (A) 48 cm
- (B) 24 cm
- (C) 12 cm
- (D) 36 cm
- 7. The sides of a triangle are 35 cm, 54 cm and 61 cm, respectively. The length of its longest altitude
  - (A)  $16\sqrt{5}$  cm
- (B)  $10\sqrt{5}$  cm (C)  $24\sqrt{5}$  cm
- (D) 28 cm
- 8. The area of an isosceles triangle having base 2 cm and the length of one of the equal sides 4 cm, is
  - (A)  $\sqrt{15}$  cm<sup>2</sup>
- (B)  $\sqrt{\frac{15}{2}} \text{ cm}^2$  (C)  $2\sqrt{15} \text{ cm}^2$  (D)  $4\sqrt{15} \text{ cm}^2$
- 9. The edges of a triangular board are 6 cm, 8 cm and 10 cm. The cost of painting it at the rate of 9 paise per cm<sup>2</sup> is
  - (A) Rs 2.00
- (B) Rs 2.16
- (C) Rs 2.48
- (D) Rs 3.00

# (C) Short Answer Questions with Reasoning

Write **True** or **False** and justify your answer:

**Sample Question 1:** If a, b, c are the lengths of three sides of a triangle, then area of a triangle =  $\sqrt{s(s-a)(s-b)(s-c)}$ , where s = perimeter of triangle.

**Solution**: False. Since in Heron's formula.

$$s = \frac{1}{2}(a+b+c)$$

$$=\frac{1}{2}$$
 (perimeter of triangle)

#### **EXERCISE 12.2**

Write **True** or **False** and justify your answer:

- 1. The area of a triangle with base 4 cm and height 6 cm is 24 cm<sup>2</sup>.
- 2. The area of  $\triangle$  ABC is 8 cm<sup>2</sup> in which AB = AC = 4 cm and  $\angle$ A = 90°.
- 3. The area of the isosceles triangle is  $\frac{5}{4}\sqrt{11}$  cm<sup>2</sup>, if the perimeter is 11 cm and the base is 5 cm.
- **4.** The area of the equilateral triangle is  $20\sqrt{3}$  cm<sup>2</sup> whose each side is 8 cm.
- **5.** If the side of a rhombus is 10 cm and one diagonal is 16 cm, the area of the rhombus is 96 cm<sup>2</sup>.
- **6.** The base and the corresponding altitude of a parallelogram are 10 cm and 3.5 cm, respectively. The area of the parallelogram is 30 cm<sup>2</sup>.
- 7. The area of a regular hexagon of side 'a' is the sum of the areas of the five equilateral triangles with side a.
- **8.** The cost of levelling the ground in the form of a triangle having the sides 51 m, 37 m and 20 m at the rate of Rs 3 per m<sup>2</sup> is Rs 918.
- **9.** In a triangle, the sides are given as 11 cm, 12 cm and 13 cm. The length of the altitude is 10.25 cm corresponding to the side having length 12 cm.

## (D) Short Answer Questions

**Sample Question 1:** The sides of a triangular field are 41 m, 40 m and 9 m. Find the number of rose beds that can be prepared in the field, if each rose bed, on an average needs 900 cm<sup>2</sup> space.

**Solution :** Let a = 41 m, b = 40 m, c = 9 m.

$$s = \frac{a+b+c}{2} = \frac{41+40+9}{2}$$
 m = 45 m

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Area of the triangular field

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{45(45-41)(45-40)(45-9)}$$

$$= \sqrt{45\times4\times5\times36} = 180 \text{ m}^2$$

So, the number of rose beds =  $\frac{180}{0.09}$  = 2000

Sample Question 2: Calculate the area of the shaded region in Fig. 12.1.

**Solution:** For the triangle having the sides 122 m, 120 m and 22 m:

$$s = \frac{122 + 120 + 22}{2} = 132$$
Area of the triangle =  $\sqrt{s(s-a)(s-b)(s-c)}$ 

$$= \sqrt{132(132 - 122)(132 - 120)(132 - 22)}$$

$$= \sqrt{132 \times 10 \times 12 \times 110}$$

$$= 1320 \text{ m}^2$$

For the triangle having the sides 22 m, 24 m and 26 m:

$$s = \frac{22 + 24 + 26}{2} = 36$$
Area of the triangle =  $\sqrt{36(36 - 22)(36 - 24)(36 - 26)}$ 

$$= \sqrt{36 \times 14 \times 12 \times 10}$$

$$= 24\sqrt{105}$$

$$= 24 \times 10.25 \text{ m}^2 \text{ (approx.)}$$

$$= 246 \text{ m}^2$$
Therefore, the area of the shaded portion
$$= (1320 - 246) \text{ m}^2$$

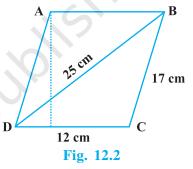
$$= 1074 \text{ m}^2$$
22 m

Fig. 12.1

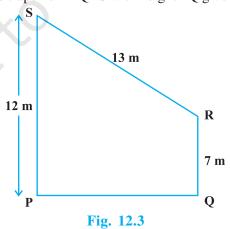
#### **EXERCISE 12.3**

1 Find the cost of laying grass in a triangular field of sides 50 m, 65 m and 65 m at the rate of Rs 7 per  $m^2$ .

- 2 The triangular side walls of a flyover have been used for advertisements. The sides of the walls are 13 m, 14 m and 15 m. The advertisements yield an earning of Rs 2000 per m<sup>2</sup> a year. A company hired one of its walls for 6 months. How much rent did it pay?
- 3 From a point in the interior of an equilateral triangle, perpendiculars are drawn on the three sides. The lengths of the perpendiculars are 14 cm, 10 cm and 6 cm. Find the area of the triangle.
- 4 The perimeter of an isosceles triangle is 32 cm. The ratio of the equal side to its base is 3 : 2. Find the area of the triangle.
- 5 Find the area of a parallelogram given in Fig. 12.2. Also find the length of the altitude from vertex A on the side DC.
- 6 A field in the form of a parallelogram has sides 60 m and 40 m and one of its diagonals is 80 m long. Find the area of the parallelogram.
- 7 The perimeter of a triangular field is 420 m and its sides are in the ratio 6:7:8. Find the area of the triangular field.
- 8 The sides of a quadrilateral ABCD are 6 cm, 8 cm, 12 cm and 14 cm (taken in order) respectively, and the angle between the first two sides is a right angle. Find its area.



- A rhombus shaped sheet with perimeter 40 cm and one diagonal 12 cm, is painted on both sides at the rate of Rs 5 per m<sup>2</sup>. Find the cost of painting.
- 10 Find the area of the trapezium PQRS with height PQ given in Fig. 12.3



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### (E) Long Answer Questions

**Sample Question 1:** If each side of a triangle is doubled, then find the ratio of area of the new triangle thus formed and the given triangle.

**Solution :** Let a, b, c be the sides of the triangle (existing) and s be its semi-perimeter.

Then, 
$$s = \frac{a+b+c}{2}$$
  
or,  $2s = a+b+c$  (1)

Area of the existing triangle = 
$$\sqrt{s(s-a)(s-b)(s-c)} = \Delta$$
, say

According to the statement, the sides of the new triangle will be 2a, 2b and 2c. Let S be the semi-perimeter of the new triangle.

$$S = \frac{2a + 2b + 2c}{2} = a + b + c \tag{2}$$

From (1) and (2), we get

$$S = 2s \tag{3}$$

Area of the new triangle

$$= \sqrt{S(S-2a)(S-2b)(S-2c)}$$

Putting the values, we get

$$= \sqrt{2s(2s-2a)(2s-2b)(2s-2c)}$$

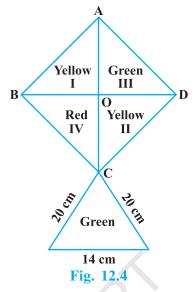
$$= \sqrt{16s(s-a)(s-b)(s-c)}$$

$$= 4\sqrt{s(s-a)(s-b)(s-c)} = 4\Delta$$

Therefore, the required ratio is 4:1.

#### **EXERCISE 12.4**

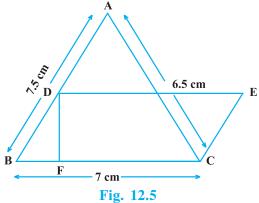
1. How much paper of each shade is needed to make a kite given in Fig. 12.4, in which ABCD is a square with diagonal 44 cm.



- 2. The perimeter of a triangle is 50 cm. One side of a triangle is 4 cm longer than the smaller side and the third side is 6 cm less than twice the smaller side. Find the area of the triangle.
- **3.** The area of a trapezium is 475 cm<sup>2</sup> and the height is 19 cm. Find the lengths of its two parallel sides if one side is 4 cm greater than the other.
- **4.** A rectangular plot is given for constructing a house, having a measurement of 40 m long and 15 m in the front. According to the laws, a minimum of 3 m, wide space should be left in the front and back each and 2 m wide space on each of other sides. Find the largest area where house can be constructed.
- **5.** A field is in the shape of a trapezium having parallel sides 90 m and 30 m. These sides meet the third side at right angles. The length of the fourth side is 100 m. If it costs Rs 4 to plough 1m<sup>2</sup> of the field, find the total cost of ploughing
- 6. In Fig. 12.5, Δ ABC has sides AB = 7.5 cm, AC = 6.5 cm and BC = 7 cm. On base BC a parallelogram DBCE of same area as that of Δ ABC is constructed. Find the height DF of the parallelogram.

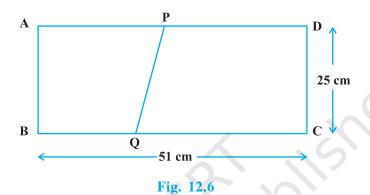
the field.

7. The dimensions of a rectangle ABCD are 51 cm × 25 cm. A trapezium PQCD with its parallel



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sides QC and PD in the ratio 9: 8, is cut off from the rectangle as shown in the Fig. 12.6. If the area of the trapezium PQCD is  $\frac{5}{6}$ th part of the area of the rectangle, find the lengths QC and PD.



**8.** A design is made on a rectangular tile of dimensions 50 cm × 70 cm as shown in Fig. 12.7. The design shows 8 triangles, each of sides 26 cm, 17 cm and 25 cm. Find the total area of the design and the remaining area of the tile.

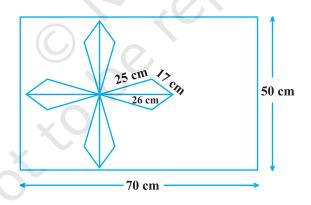


Fig. 12.7