# Chapter Thirteen

# KINETIC THEORY



## MCQ I

- 13.1 A cubic vessel (with faces horizontal + vertical) contains an ideal gas at NTP. The vessel is being carried by a rocket which is moving at a speed of  $500 \text{m s}^{-1}$  in vertical direction. The pressure of the gas inside the vessel as observed by us on the ground
  - (a) remains the same because  $500 \mathrm{m \, s^{-1}}$  is very much smaller than  $v_{rms}$  of the gas.
  - (b) remains the same because motion of the vessel as a whole does not affect the relative motion of the gas molecules and the walls.
  - (c) will increase by a factor equal to  $(v_{ms}^2 + (500)^2)/v_{ms}^2$  where  $v_{ms}$  was the original mean square velocity of the gas.
  - (d) will be different on the top wall and bottom wall of the vessel.
- 13.2 1 mole of an ideal gas is contained in a cubical volume *V*, ABCDEFGH at 300 K (Fig. 13.1). One face of the cube (EFGH) is made up of a material which totally absorbs any gas molecule

incident on it. At any given time,

- (a) the pressure on EFGH would be zero.
- (b) the pressure on all the faces will the equal.
- (c) the pressure of EFGH would be double the pressure on ABCD.
- (d) the pressure on EFGH would be half that on ABCD.

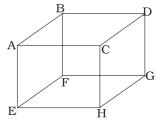


Fig. 13.1

- **13.3** Boyle's law is applicable for an
  - (a) adiabatic process.
  - (b) isothermal process.
  - (c) isobaric process.
  - (d) isochoric process.
- 13.4 A cylinder containing an ideal gas is in vertical position and has a piston of mass *M* that is able to move up or down without friction (Fig. 13.2). If the temperature is increased,

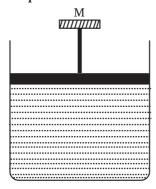


Fig. 13.2

- (a) both p and V of the gas will change.
- (b) only *p* will increase according to Charle's law.
- (c) V will change but not p.
- (d) *p* will change but not *V*.
- Volume versus temperature graphs for a given mass of an ideal gas are shown in Fig. 13.3 at two different values of constant pressure. What can be inferred about relation between  $P_1$  &  $P_2$ ?

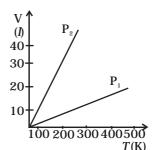


Fig.13.3

- (a)  $P_1 > P_2$
- (b)  $P_1 = P_2$
- (c)  $P_1 < P_2$
- (d) data is insufficient.

- 13.6 1 mole of  $H_0$  gas is contained in a box of volume  $V = 1.00 \text{ m}^3$  at T = 300K. The gas is heated to a temperature of T = 3000K and the gas gets converted to a gas of hydrogen atoms. The final pressure would be (considering all gases to be ideal)
  - (a) same as the pressure initially.
  - (b) 2 times the pressure initially.
  - (c) 10 times the pressure initially.
  - (d) 20 times the pressure initially.
- A vessel of volume *V* contains a mixture of 1 mole of Hydrogen 13.7 and 1 mole of Oxygen (both considered as ideal). Let  $f_i(v)dv$ , denote the fraction of molecules with speed between v and (v + dv) with  $f_{2}(v)dv$ , similarly for oxygen. Then
  - (a)  $f_1(v) + f_2(v) = f(v)$  obeys the Maxwell's distribution law.
  - (b)  $f_1(v)$ ,  $f_2(v)$  will obey the Maxwell's distribution law separately.
  - (c) Neither  $f_1$  (v), nor  $f_2$  (v) will obey the Maxwell's distribution
  - (d)  $f_2$  (v) and  $f_1$  (v) will be the same.
- 13.8 An inflated rubber balloon contains one mole of an ideal gas, has a pressure p, volume V and temperature T. If the temperature rises to 1.1 T, and the volume is increaset to 1.05 V, the final pressure will be
  - (a) 1.1 p
  - (b) p
  - (c) less than p
  - (d) between p and 1.1.

# MCQ II

13.9

ABCDEFGH is a hollow cube made of an insulator (Fig. 13.4). Face ABCD has positve charge on it. Inside the cube, we have ionized hydrogen.

The usual kinetic theory expression for pressure

- (a) will be valid.
- (b) will not be valid since the ions would experience forces other than due to collisions with the walls.
- (c) will not be valid since collisions with walls would not be elastic.
- (d) will not be valid because isotropy is lost.
- Fig. 13.4

В

+P

F

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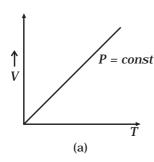
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13.10

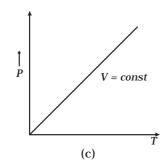
Diatomic molecules like hydrogen have energies due to both translational as well as rotational motion. From the equation in

kinetic theory  $pV = \frac{2}{3}E$ , E is

- (a) the total energy per unit volume.
- (b) only the translational part of energy because rotational energy is very small compared to the translational energy.
- (c) only the translational part of the energy because during collisions with the wall pressure relates to change in linear momentum.
- (d) the translational part of the energy because rotational energies of molecules can be of either sign and its average over all the molecules is zero.
- **13.11** In a diatomic molecule, the rotational energy at a given temperature
  - (a) obeys Maxwell's distribution.
  - (b) have the same value for all molecules.
  - (c) equals the translational kinetic energy for each molecule.
  - (d) is (2/3)rd the translational kinetic energy for each molecule.
- **13.12** Which of the following diagrams (Fig. 13.5) depicts ideal gas behaviour?



 $\uparrow P \qquad T = const$ (b)



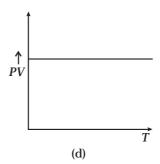


Fig. 13.5

- **13.13** When an ideal gas is compressed adiabatically, its temperature rises: the molecules on the average have more kinetic energy than before. The kinetic energy increases,
  - (a) because of collisions with moving parts of the wall only.
  - (b) because of collisions with the entire wall.

- (c) because the molecules gets accelerated in their motion inside the volume.
- (d) because of redistribution of energy amongst the molecules.

### **VSA**

- **13.14** Calculate the number of atoms in 39.4 g gold. Molar mass of gold is 197g mole<sup>-1</sup>.
- **13.15** The volume of a given mass of a gas at 27°C, 1 atm is 100 cc. What will be its volume at 327°C?
- 13.16 The molecules of a given mass of a gas have root mean square speeds of  $100\,\mathrm{m\,s^{-1}}$  at  $27\,^{\circ}\mathrm{C}$  and 1.00 atmospheric pressure. What will be the root mean square speeds of the molecules of the gas at  $127\,^{\circ}\mathrm{C}$  and 2.0 atmospheric pressure?
- 13.17 Two molecules of a gas have speeds of  $9 \times 10^6 \, m \, s^{-1}$  and  $1 \times 10^6 \, m \, s^{-1}$ , respectively. What is the root mean square speed of these molecules.
- **13.18** A gas mixture consists of 2.0 moles of oxygen and 4.0 moles of neon at temperature *T*. Neglecting all vibrational modes, calculate the total internal energy of the system. (Oxygen has two rotational modes.)
- 13.19 Calculate the ratio of the mean free paths of the molecules of two gases having molecular diameters  $1\,\mathring{A}$  and  $2\,\mathring{A}$ . The gases may be considered under identical conditions of temperature, pressure and volume.

#### SA

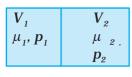


Fig 13.6

- 13.20 The container shown in Fig. 13.6 has two chambers, separated by a partition, of volumes  $V_1 = 2.0$  litre and  $V_2 = 3.0$  litre. The chambers contain  $\mu_1 = 4.0$  and  $\mu_2 = 5.0$  moles of a gas at pressures  $p_1 = 1.00$  atm and  $p_2 = 2.00$  atm. Calculate the pressure after the partition is removed and the mixture attains equilibrium.
- 13.21 A gas mixture consists of molecules of types A, B and C with masses  $m_A > m_B > m_C$ . Rank the three types of molecules in decreasing order of (a) average K.E., (b) rms speeds.

- 13.22 We have 0.5 g of hydrogen gas in a cubic chamber of size 3cm kept at NTP. The gas in the chamber is compressed keeping the temperature constant till a final pressure of 100 atm. Is one justified in assuming the ideal gas law, in the final state?
  - (Hydrogen molecules can be consider as spheres of radius 1  $\overset{o}{\rm A}$  ).
- **13.23** When air is pumped into a cycle tyre the volume and pressure of the air in the tyre both are increased. What about Boyle's law in this case?
- **13.24** A ballon has 5.0 g mole of helium at 7°C. Calculate
  - (a) the number of atoms of helium in the balloon,
  - (b) the total internal energy of the system.
- **13.25** Calculate the number of degrees of freedom of molecules of hydrogen in 1 cc of hydrogen gas at NTP.
- **13.26** An insulated container containing monoatomic gas of molar mass m is moving with a velocity  $v_o$ . If the container is suddenly stopped, find the change in temperature.

### LA

- **13.27** Explain why
  - (a) there is no atmosphere on moon.
  - (b) there is fall in temperature with altitude.
- **13.28** Consider an ideal gas with following distribution of speeds.

| Speed (m/s) | % of molecules |
|-------------|----------------|
| 200         | 10             |
| 400         | 20             |
| 600         | 40             |
| 800         | 20             |
| 1000        | 10             |

- (i) Calculate  $V_{rms}$  and hence T. ( $m = 3.0 \times 10^{-26} \text{kg}$ )
- (ii) If all the molecules with speed 1000 m/s escape from the system, calculate new  $V_{\rm rms}$  and hence T.

- 13.29 Ten small planes are flying at a speed of 150 km/h in total darkness in an air space that is  $20 \times 20 \times 1.5 \text{ km}^3$  in volume. You are in one of the planes, flying at random within this space with no way of knowing where the other planes are. On the average about how long a time will elapse between near collision with your plane. Assume for this rough computation that a saftey region around the plane can be approximated by a sphere of radius 10m.
- **13.30** A box of 1.00m³ is filled with nitrogen at 1.50 atm at 300K. The box has a hole of an area 0.010 mm². How much time is required for the pressure to reduce by 0.10 atm, if the pressure outside is 1 atm.
- 13.31 Consider a rectangular block of wood moving with a velocity  $v_0$  in a gas at temperature T and mass density  $\rho$ . Assume the velocity is along x-axis and the area of cross-section of the block perpendicular to  $v_0$  is A. Show that the drag force on the block is  $4\rho A v_0 \sqrt{\frac{kT}{m}}$ , where m is the mass of the gas molecule.